Homework 2 (MATH 2310-04)

Due date: Thursday, Feb. 13, 2014

1. Solve the given differential equations:

a)
$$\frac{dy}{dx} + y^{2} \sin(x) = 0$$

b)
$$\frac{dy}{dx} = \frac{x^{2}}{y(1+x^{3})}$$

2. Solve the following initial value problem and determine where the solution attains its maximum value.

$$\frac{dy}{dx} = \frac{2 - e^x}{3 + 2y}$$
 $y(0) = 0$

3. A tank initially contains 120 liters of pure water. A mixture containing a concentration of γ g/liter of salt enters the tank at a rate of 2 liters /min, and the well-stirred mixture leaves the tank at the same rate. Find an expression in terms of γ for the amount of salt in the tank at any time t. Also find the limiting amount of salt in the tank as t $\rightarrow \infty$.