

Homework 4 (MATH 5400-01)**Name (Print):****Due date: Friday, Oct. 5, 2012**

1. Solve formally by separation of variables:

$$\begin{aligned}u_{tt} &= c^2 u_{xx}, & 0 < x < L, t > 0 \\u(x, 0) &= f(x), \quad u_t(x, 0) = g(x), & 0 \leq x \leq L \\u(0, t) &= 0, \quad u_x(L, t) = 0, & t \geq 0\end{aligned}$$

2. Solve formally by separation of variables:

$$\begin{aligned}u_{tt} + k u_t &= c^2 u_{xx} + F(x, t), & 0 < x < L, t > 0 \\u(x, 0) &= 0, \quad u_t(x, 0) = 0, & 0 \leq x \leq L \\u(0, t) &= 0, \quad u_x(L, t) = 0, & t \geq 0\end{aligned}$$

3. Solve this problem:

$$\begin{aligned}u_{tt} &= c^2 u_{xx}, & 0 < x < 1, t > 0 \\u(x, 0) &= x + 1, \quad u_t(x, 0) = x(1 - x), & 0 \leq x \leq 1 \\u(0, t) &= 1, \quad u(1, t) = 2, & t \geq 0\end{aligned}$$

Hint: Introduce $v = u - U$, where $U(x)$ satisfies the boundary conditions. Calculate v by solving its PDE.