

Homework 6 (MATH 5400-01)**Name (Print):****Due date: Friday, Oct. 19, 2012**

1. Solve this problem ($r = |\mathbf{x}|$):

$$\begin{aligned}u_{tt} &= c^2 \Delta u, & \mathbf{x} \in \mathbb{R}_3, t > 0 \\u(\mathbf{x}, 0) &= r, \quad u_t(\mathbf{x}, 0) = 1, & \mathbf{x} \in \mathbb{R}_3\end{aligned}$$

2. Solve this problem by specifying Kirchhoff's formula:

$$\begin{aligned}u_{tt} &= c^2 \Delta u, & \mathbf{x} \in \mathbb{R}_3, t > 0 \\u(\mathbf{x}, 0) &= \delta(\mathbf{x}), \quad u_t(\mathbf{x}, 0) = 1, & \mathbf{x} \in \mathbb{R}_3\end{aligned}$$

Hint: use $z \delta'(z) = -\delta(z)$ to simplify the solution.