

**Homework 1 (MATH 4300-01)**  
**Due date: Friday, Sept. 13, 2013**

**Name (Print):**

1. Consider the following data.

$x$	1	2	3	4	5	6	7
$y$	100	25	11	6	4	3	2

- Plot  $\ln y$  versus  $x$  and  $\ln x$ . Compare the data with a linear function if one of these plots supports the use of a linear function.
- Graph the table data and the model that follows from the above relation.
- Calculate the relative error of your model in %.
- At which  $x$  is the value of  $y$  at  $x = 2.5$  reduced by 25%?

2. Consider the following data.

$x$	1	2	3	4	5	6	7
$y$	2	35	150	500	1250	2500	5000

- Plot  $\ln y$  versus  $x$  and  $\ln x$ . Compare the data with a linear function if one of these plots supports the use of a linear function.
- Graph the table data and the model that follows from the above relation.
- Calculate the relative error of your model in %.
- At which  $x$  is the value of  $y$  at  $x = 2.5$  increased by 150%?

3. The U.S. Bureau of Public Roads determined the following total stopping distances  $D$  (in ft) depending on the velocity  $v$  (in mph) of cars.

$v$	20	30	40	50	60	70	80
$D$	42	73.5	116	173	248	343	464

- Use the data to plot  $\ln D$  versus  $v$  and  $\ln v$ . Compare the data with linear functions that reveal the parameters of corresponding exponential and power function models.
- Use the data to plot  $D / v$ . Compare the data with a linear and a quadratic function.
- Plot  $D$  according to the original data in comparison to the two models for  $D / v$ . Calculate the relative error of the two polynomial models.
- Discuss the suitability of the models obtained for  $D$ . Identify one model that provides a formula that can be used to calculate the total stopping distance without using a calculator. Illustrate the use of this formula by three examples.