

POTENTIAL GAINS FROM TRADING

BAD OUTPUTS: The case of U.S.

electric power plants

by

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INTRODUCTION

Coal-fired electric power plants

produce, in addition to good output

(kwh) multiple bad outputs (CO_2 ,

NO_x and SO_2)

We investigate the impact on good

output production by allowing for trade

of individual bads (and combinations

of them), while regulating the industry

bad outputs. We set the latter to

the total observed amounts.

POLLUTING TECHNOLOGIES

$x \in \mathbb{R}_+^N$ input vector

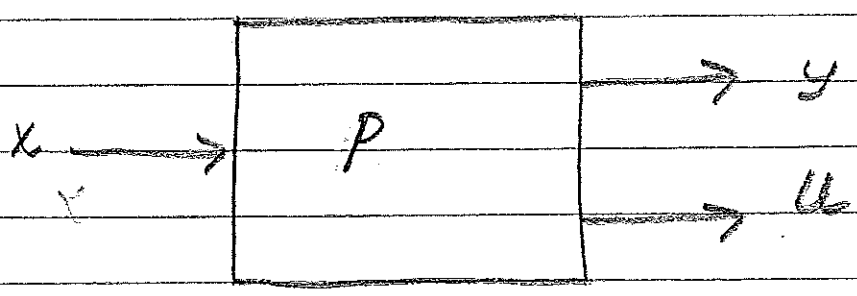
$y \in \mathbb{R}_+^M$ desirable output vector

$u \in \mathbb{R}_+^J$ bad undesirable output vector

} divisibility

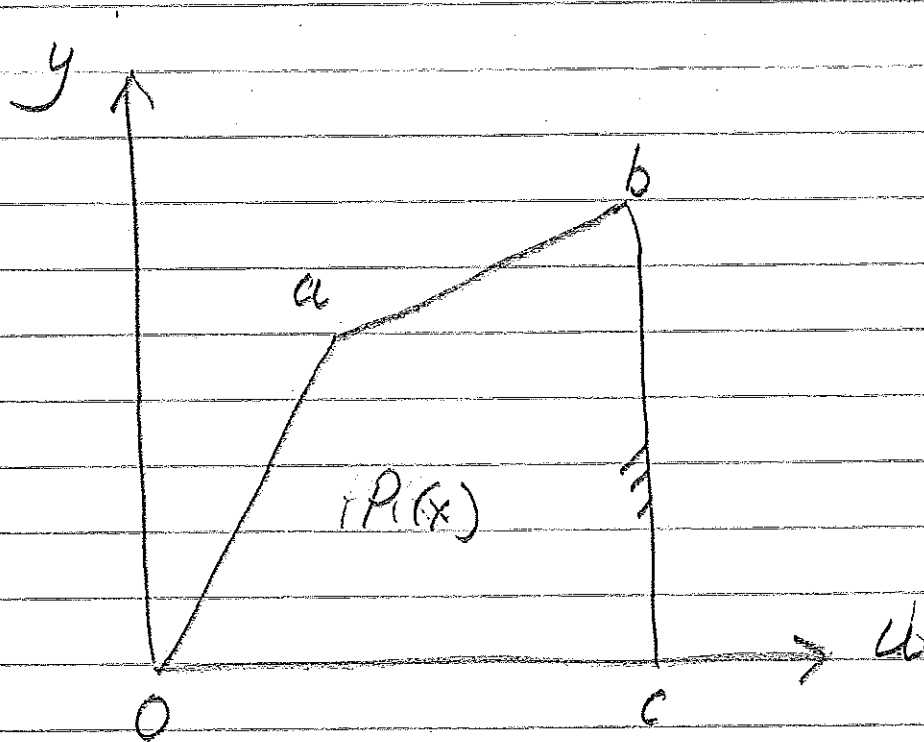
$$P(x) = \{ (y, u) : x \text{ can produce } (y, u) \}$$

the 'output set, technology



The black box

(one may go into the black box by modeling the technology as a network)



An Output Set

1. Nulljointness $(y, u) \in P(x), u=0 \Rightarrow y=0$

2. Weak disposability of (y, u)

$$(y, u) \in P(x), 0 \leq \theta \leq 1 \Rightarrow (\theta y, \theta u) \in P(x)$$

3. Strong (free) disposability of y

$$(y, u) \in P(x), y' \leq y \Rightarrow (y', u) \in P(x)$$

Additional standard axioms.

The Activity Analysis / Data Envelopment

(DEA) Formulation

$R=1, \dots, K$ observations of (x, y, u) at each

$t=1, \dots, T,$

$$P^t(x^t) = \{ (y^t, x^t) : \sum_{k=1}^K z_k^t y_{km}^t \leq y_m^t, m=1, \dots, M, \}$$

$$\sum_{k=1}^K z_k^t u_{kj}^t \leq u_j^t, j=1, \dots, J,$$

$$\sum_{k=1}^K z_k^t x_{kn}^t \leq x_n^t, n=1, \dots, N,$$

$$\{ z_k^t \geq 0 \}$$

1. $\sum_{j=1}^J u_{ij} > 0$, $\sum_{i=1}^K u_{ij} > 0$ null jointness

2. $\sum_{i=1}^M y_m^t$ and $\sum_{i=1}^K u_{ij}^t$ weak disposability

3. $\sum_{i=1}^M y_m^t$ strong disposability of good outputs

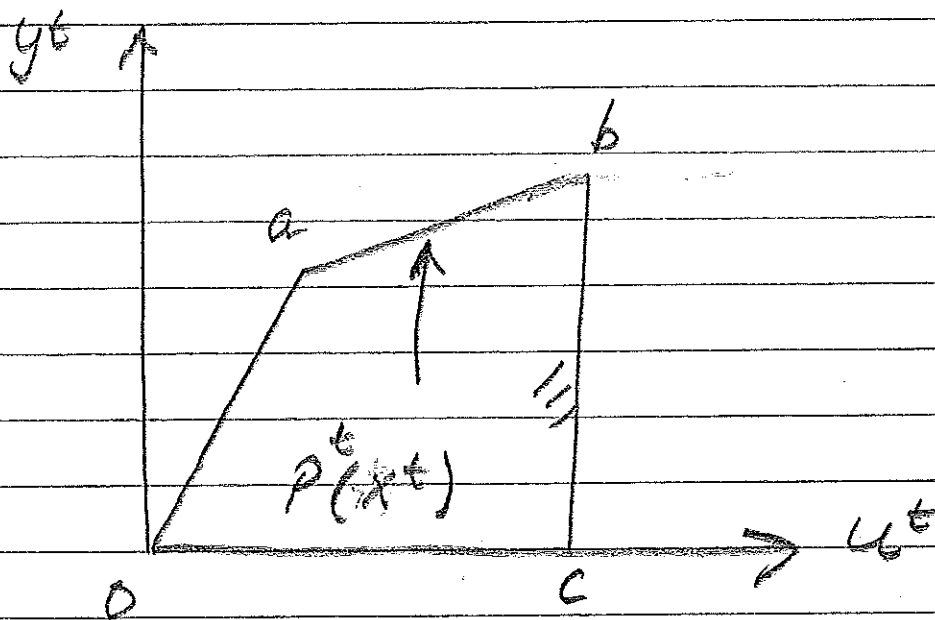
4. $\sum_{i=1}^K x_n^t$ strong disposability of inputs

5. $\sum_{i=1}^L z_i^t \geq 0$, constant returns to scale

Objective Function

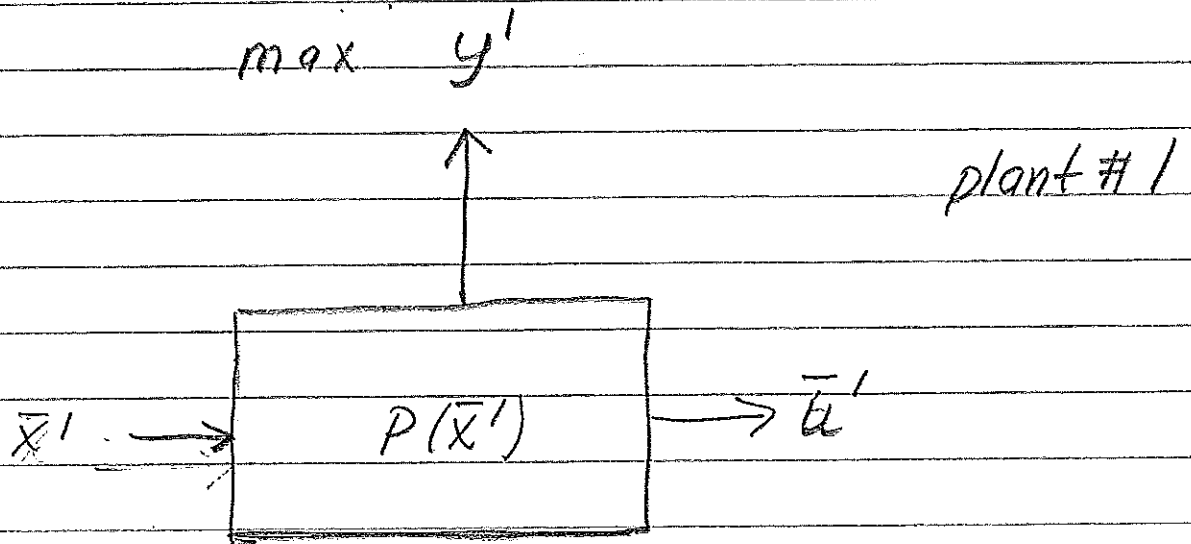
$$M=1$$

$$\max y^t \text{ s.t. } (y^t, u^t) \in P^t(x^t)$$



maximize feasible output,
given input and bad outputs

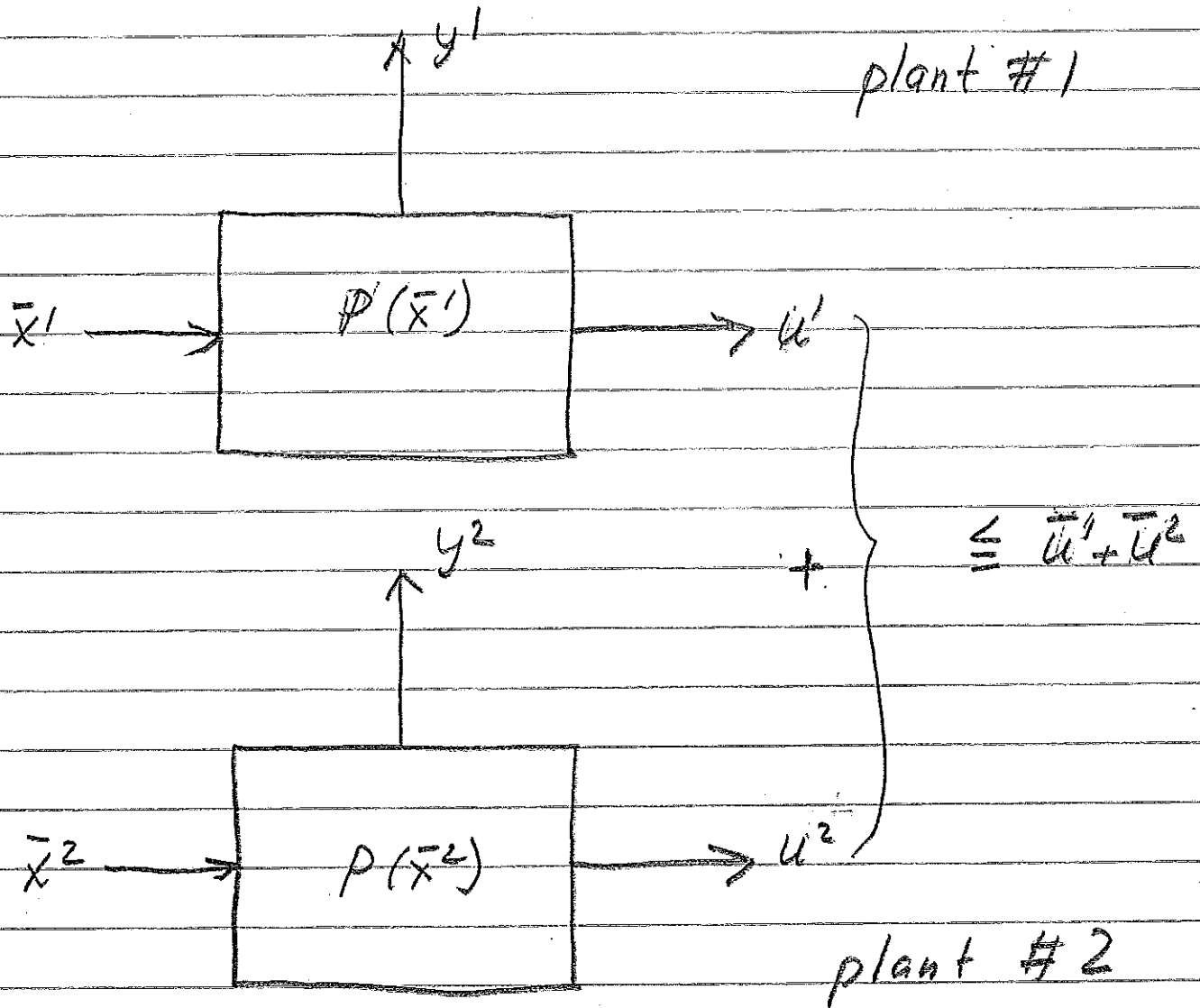
COMMAND AND CONTROL



\bar{x}' , \bar{u}' observed inputs and bad outputs

$$y^{cc} = \sum_{k=1}^k \max y^k$$

TRADING BADS



$$y_j^{TP} = \max y^1 + y^2$$

Data Sources

- Sample: coal-fired power plants in 1995-2005
 - At least 95 percent of BTUs from coal
 - 80 power plants in sample
 - Good output: net electricity generation (in kWh) from EIA-767 survey (from EIA-767 survey)
 - Bad outputs: CO₂, NO_x, and SO₂ emissions (from EPA Continuous Emissions Monitoring System, CEMS).

- Inputs
 - Capital: value of plant and equipment (derived using data from FERC Form 1 and EIA-412 surveys)
 - Labor: number of employees (from FERC Form 1 and EIA-412 surveys)
 - Fuel: consumption of coal, oil, and natural gas (in BTUs) from EIA-767 survey

RESULTS

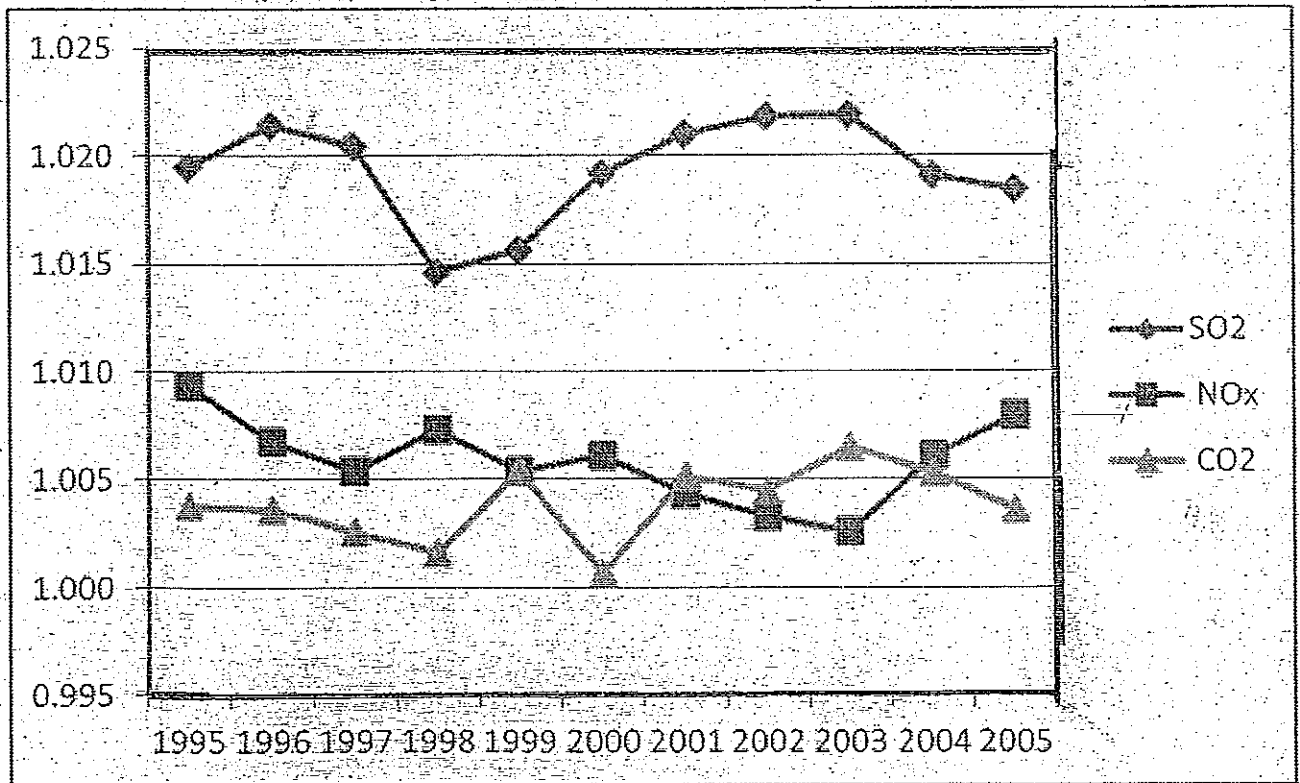


Figure 1. Annual Ratios of $\frac{Y_j^{TR}}{Y_{j0}}$
 $j=1, 2, 3$

RESULTS

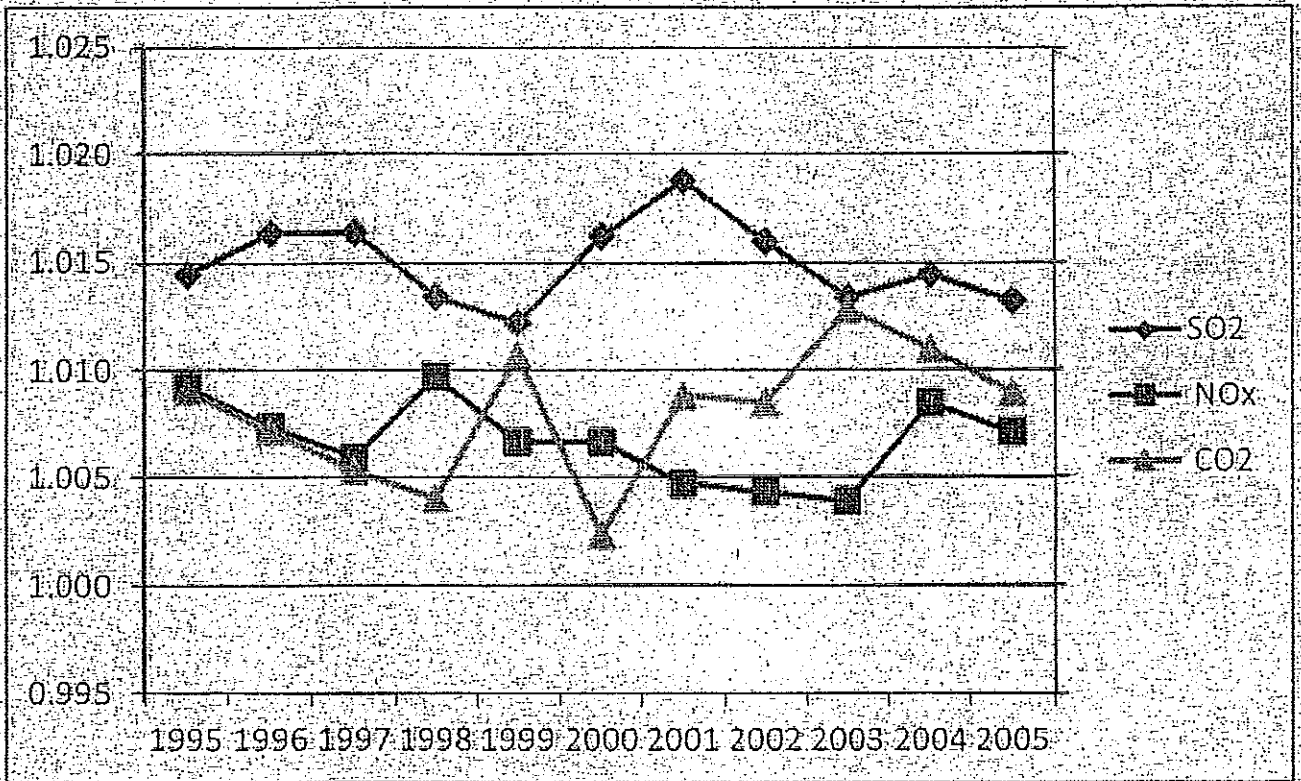
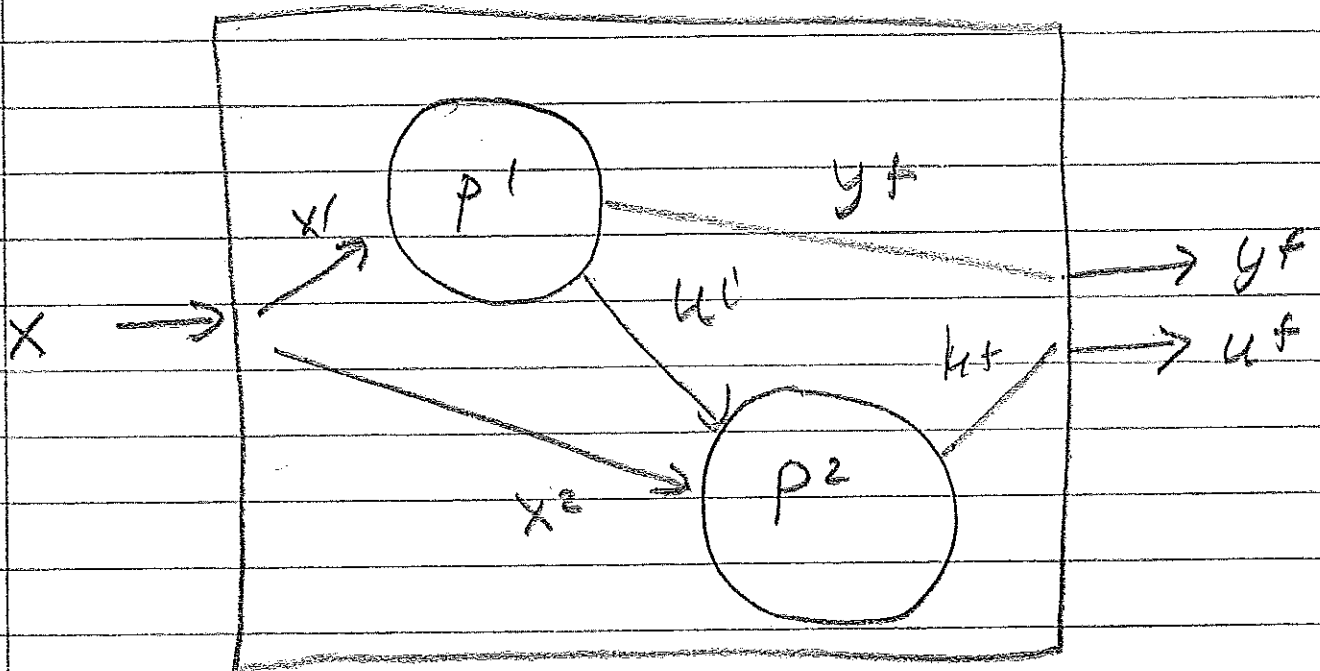


Figure 2. Annual Geometric Means of Y_j^{TP} / Y_j^{CC} , $j=1, \dots, 3$.

MODELING GOOD AND BAD

OUTPUTS IN A NETWORK



P^1 subtechnology 1

P^2 ——— 2

$$X = x^1 + x^2$$

(y^+, u^+) final output

u^i intermediate output