## AGGREGATES

## Section 7 - Quality Assurance and Quality Acceptance

## Quality Assurance

$>$ Definition: a systematic method for sampling, testing and evaluating material to assure specification compliance. Includes incentives and disincentives
$>$ Composed of:

- Quality Control (QC)
- Quality Acceptance (QA)


## Quality Assurance (continued)

$>$ Quality Control - A systematic procedure to sample, test and monitor production. Generally a contractor responsibility.
$>$ Quality Acceptance - A statistical method for evaluating compliance.

- Gradation - "Percent within limits" approach
- Quality Index > Quality Level > Pay Factor
- Compaction - "Percent above limit" approach
- Quality Index > Pay Factor


## Acceptance Methods

$>$ Representative Sample - Traditional

- Pass-Fail
- Limited Information
- Ex. 30 pound Sample for 1000 tons, How much material is really out-ofspecification?
- 2,000,000 lbs/30lbs $=\mathbf{6 6 , 6 6 7}$ samples
- No Information on Variability


## Acceptance Methods (continued)

>Sample Average

- 5 (3 to 7) Gradation Samples
- Pass-Fail based on multiple Samples \& percent within limits
- Shows Distribution
- Rewards Consistency in Practice
- Use Tighter Specs for Job Mix Design


## Acceptance Methods (continued)

Example - Grading A Plant Mix Paving
Normal Range for \#4 is 45-65\%
Have Reduced Acceptance Limits on Specific Jobs based on JMF Target $\pm 5 \%$,

For example $52 \pm 5 \% \quad(47-52-57)$
So, the Narrow Band is:
Upper Specification Limit = 57
Lower Specification Limit = 47

## Acceptance Methods (continued)

> Statistical Method

- Determine $\overline{\mathbf{x}}$ and s from data
- Define Material Assuming It Has a "Normal Probability" Distribution
- Contractor Gets Paid for \% of Materials within the Upper and Lower Specification Limits


## Acceptance Methods (continued)

>Historically, basis from W. Edwards Deming (A Wyoming native from Cody and Powell, UW Graduate in Engineering in 1921)
$>$ WYDOT has used procedure since

- 1984 in field
- 1974 in lab
>How does the System work?


## Quality Acceptance for Gradations

>For Gradations, Quality is based on the "Percentage of aggregate within specification limits".
>Example:

- Grading W
- \#4-45-65\%
- \#8 - 33-53\%
- \#200-3-12\%
- Based on - \#4
- If all of the stockpile was between 45\% and 65\%, Full Pay

Table 803.4.4-1
Gradation Requirements: Subbase and Base


## Quality Acceptance for Gradations

> How do we determine if a stockpile has between 45\% and $65 \%$ passing the \#4?
> We could go out and obtain 1000 samples and test them. This would give a very accurate picture of the $-\# 4$ fraction of the pile.
$>$ We could draw a picture of this distribution of -\#4 values, shown as the green boxes.

| \%Passing <br> Range | No. of Tests |
| :---: | :---: |
| $35-40$ | 10 |
| $40-45$ | 100 |
| $45-50$ | 300 |
| $50-55$ | 350 |
| $55-60$ | 150 |
| $60-65$ | 90 |
| $65-70$ | 0 |



## Quality Acceptance for Gradations

$>$ The red lines are the upper and lower specification limits of $45 \%$ and $65 \%$
$>$ There are 110 samples out of 1000 (11\%) that fall outside of the limits.
$>$ Since Quality is defined as the percentage of material within the specification limits,
The Contractor would
 be paid for $89 \%$ of the material.

## Quality Acceptance for Gradations

$>$ However, it is not feasible to obtain 1000 samples of a pile, so another technique is needed.
$>$ If the width of the bins was smaller, say $2 \%$ instead of 5\%, we would see a much smoother curve develop.
$>$ It has a "bell" like shape and is known as the "Normal Probability Distribution Curve"
> It can be defined by two values, the "average ${ }_{10}$, or "mean" and the "standard deviation".


# Properties of the Normal Probability Curve 

The total area under the curve is $100 \%$, which means that all the tests will be included under the curve mathematically.
$>$ The $\overline{\mathbf{x}}$ value at the peak is the mean or average value. Half the area is above the mean and half is below.
$>34.1 \%$ of the area is under the curve from zero to one Standard Deviation.
$\Rightarrow$ About 2/3 of the data is between +1 and -1 SD
$84.1 \%$ (50\% + 34.1\%) of the area is below the curve and less than 1.0 Standard Deviation.

We will assume this curve represents the pile.

Normal Probability Curve


## Quality Assurance

## $>$ Let's select 5 values out of the 1000 tests.



|  | X | ( $\mathrm{x}-\overline{\mathrm{x}}$ ) |  | $(x-\bar{x})^{2}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 53 | $=53.0-51.4=$ | 1.6 | $=1.6$ * $1.6=$ | 2.56 |
| 2 | 50 | $=50.0-51.4=$ | -1.4 | $=-1.4{ }^{*}-1.4=$ | 1.96 |
| 3 | 60 | $=60.0-51.4=$ | 8.6 | $=8.6$ * $8.6=$ | 73.96 |
| 4 | 46 | $=46.0-51.4=$ | -5.4 | $=-5.4 *-5.4=$ | 29.16 |
| 5 | 48 | $=48.0-51.4=$ | -3.4 | $=-3.4 *$-3.4 $=$ | 11.56 |
| Sum $=$ | 257.0 | $\Sigma(x-\bar{x})=$ | 0.0 | $\Sigma(x-\bar{x})^{2}=$ | 119.2 |

Standard Deviation =
$s=\sqrt{\frac{\sum(x-\bar{x})^{2}}{n-1}}$
$s=\sqrt{\frac{119.2}{5-1}}=5.46$

## Quality Assurance

$>$ We now have the Mean ( $\mathrm{X}=51.4$ ) and Standard Deviation ( $s=5.46$ ) to describe the "Normal Probability Distribution Curve"
$>$ We need to relate the area under the curves in both diagrams.
$>$ The upper and lower Specification Limits are $\mathrm{SL}_{\mathrm{u}}=65$ and $\mathrm{SL}_{\mathrm{I}}=45$.

Normal Probability Curve


## $>$ We can relate the specification limits to the standard deviations by the Quality Index.


$>$ Remember, we are trying to determine the percentage of material between the upper and lower specification limits.
$>$ The area less than the upper specification limit is a function of the Upper Quality Index, $Q_{u}=2.49$.

Normal Probability Curve

$>$ Table 113.1-1 relates Quality Indices to the remaining area, $P_{u}$.

Table 113.1-1
Quality Level Analysis by the Standard Deviation Method

| $P_{U}$ or $P_{L}$ percent Within Limits for Positive Values of $\mathrm{CO} \mathrm{Q}_{\mathrm{L}}$ | Upper Quality Index $Q_{U}$ or Lower Quality Index |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{n}=3$ | $\mathrm{n}=4$ | $n=5$ | $\mathrm{n}=6$ | $\mathrm{n}=7$ |
| 100 | 1.16 | 1.50 | 1.79 | 2.03 | 2.23 |
| 90 |  | 1.47 | 4.87 | 1.80 | 1.89 |
| 98 | 1.15 | 1.44 | 1.60 | 1.70 | 1.76 |
| 97 |  | 1.41 | 1.54 | 1.62 | 1.67 |
| 96 | 1. 14 | 1.38 | 1.49 | 1.55 | 1.59 |
| 95 |  | 1.35 | 1.44 | 1.49 | 1.52 |
| 94 | 1.13 | 1.32 | 1.39 | 1.43 | 1.46 |
| 93 |  | 1.29 | 1.35 | 1.38 | 1.40 |
| 92 | 1.12 | 1.26 | 1.31 | 1.33 | 1.35 |
| 91 | 1.11 | 1.23 | 1.27 | 1.29 | 1.30 |
| 90 | 1.10 | 1.20 | 1.23 | 1.24 | 1.25 |
| 89 | 1.09 | 1.17 | 1.19 | 1.20 | 1.20 |
| 88 | 1.07 | 1.14 | 1.15 | 1.16 | 1.16 |
| 87 | 1.06 | 1.11 | -1.12 | 1.12 | 1.12 |
| 86 | 1.04 | 1.08 | 1.08 | 1.08 | 1.08 |
| 85 | 1.03 | 1.05 | 1.05 | 1.04 | 1.04 |
| 84 | 1.01 | 1.02 | 1.01 | 1.01 | 1.00 |
| 83 | 1.00 | 0.99 | 0.98 | 0.97 | 0.97 |
| 82 | 0.97 | 0.96 | 0.95 | 0.94 | 0.93 |
| 81 | 0.96 | 0.93 | 0.91 | 0.90 | 0.90 |
| 80 | 0.93 | 0.90 | 0.88 | 0.87 | 0.86 |
| 79 | 0.91 | 0.87 | 0.85 | 0.84 | 0.83 |
| 78 | 0.89 | 0.84 | 0.82 | 0.80 | 0.80 |
| 77 | 0.87 | 0.81 | 0.78 | 0.77 | 0.76 |
| 76 | 0.84 | 0.78 | 0.75 | 0.74 | 0.73 |
| 75 | 0.82 | 0.75 | 0.72 | 0.71 | 0.70 |
| 74 | 0.79 | 0.72 | 0.69 | 0.68 | 0.67 |
| 73 | 0.76 | 0.69 | 0.66 | 0.65 | 0.64 |
| 72 | 0.74 | 0.66 | 0.63 | 0.62 | 0.61 |
| 71 | 0.71 | 0.63 | 0.60 | 0.59 | 0.58 |
| 70 | 0.68 | 0.60 | 0.57 | 0.56 | 0.55 |
| 69 | 0.65 | 0.57 | 0.54 | 0.53 | 0.52 |
| 68 | 0.62 | 0.54 | 0.51 | 0.50 | 0.49 |
| 67 | 0.59 | 0.51 | 0.47 | 0.47 | 0.46 |
| 66 | 0.56 | 0.48 | 0.45 | 0.44 | 0.44 |


|  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $P_{U}$ or $P_{L}$ percent <br> Within Limits for <br> Positive Values of <br> $Q_{U}$ or $Q_{L}$ |  |  |  |  |  |
|  | $n=3$ | $n=4$ | $n=5$ | $n=6$ | $n=7$ |
| 65 | 0.52 | 0.45 | 0.43 | 0.41 | 0.41 |
| 64 | 0.49 | 0.42 | 0.40 | 0.39 | 0.38 |
| 63 | 0.46 | 0.39 | 0.37 | 0.36 | 0.35 |
| 62 | 0.43 | 0.36 | 0.34 | 0.33 | 0.32 |
| 61 | 0.39 | 0.33 | 0.31 | 0.30 | 0.30 |
| 60 | 0.36 | 0.30 | 0.28 | 0.27 | 0.27 |
| 59 | 0.32 | 0.27 | 0.25 | 0.25 | 0.24 |
| 58 | 0.29 | 0.24 | 0.23 | 0.22 | 0.21 |
| 57 | 0.25 | 0.21 | 0.20 | 0.19 | 0.19 |
| 56 | 0.22 | 0.18 | 0.17 | 0.16 | 0.16 |
| 55 | 0.18 | 0.15 | 0.14 | 0.13 | 0.13 |
| 54 | 0.14 | 0.12 | 0.11 | 0.11 | 0.11 |
| 53 | 0.11 | 0.09 | 0.08 | 0.08 | 0.08 |
| 52 | 0.07 | 0.06 | 0.06 | 0.05 | 0.05 |
| 51 | 0.04 | 0.03 | 0.03 | 0.03 | 0.03 |
| 50 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |
|  |  |  |  |  |  |

$>$ The area greater than the lower specification limit is a function of the Lower Quality Index, $Q_{1}=1.17$.
$>$ Table 113.1-1 shows $P_{I}=89 \%$.

$>$ Note that was the same area as we found with the 1000 samples!

Table 113.1-1
Quality Level Analysis by the Standard Deviation Method

| $P_{U}$ or $P_{L}$ percent Within Limits for Positive Values of $Q_{U}$ or $Q_{L}$ | Upper Quality Index $Q_{U}$ or Lower Quality Index |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{n}=3$ | $\mathrm{n}=4$ | $\mathrm{n}=5$ | $\mathrm{n}=6$ | $\mathrm{n}=7$ |
| 100 | 1.16 | 1.50 | 1.79 | 2.03 | 2.23 |
| 99 |  | 1.47 | 1.67 | 1.80 | 1.89 |
| 98 | 1.15 | 1.44 | 1.60 | 1.70 | 1.76 |
| 97 |  | 1.41 | 1.54 | 1.62 | 1.67 |
| 96 | 1. 14 | 1.38 | 1.49 | 1.55 | 1.59 |
| 95 |  | 1.35 | 1.44 | 1.49 | 1.52 |
| 94 | 1.13 | 1.32 | 1.39 | 1.43 | 1.46 |
| 93 |  | 1.29 | 1.35 | 1.38 | 1.40 |
| 92 | 1.12 | 1.26 | 1.31 | 1.33 | 1.35 |
| 91 | 1.11 | 1.23 | 1.27 | 1.29 | 1.30 |
| 90 | 1.10 | 1.20 | 1.20 | 1.24 | 1.25 |
| 89 | 1.09 | 1.17 | 1.19 | 1.20 | 1.20 |
| 88 | 1.07 | 1.14 | 1.15 | 1.16 | 1.16 |
| 87 | 1.06 | 1.11 | 112 | 1.12 | 1.12 |
| 86 | 1.04 | 1.08 | 1.08 | 1.08 | 1.08 |
| 85 | 1.03 | 1.05 | 1.05 | 1.04 | 1.04 |
| 84 | 1.01 | 1.02 | 1.01 | 1.01 | 1.00 |
| 83 | 1.00 | 0.99 | 0.98 | 0.97 | 0.97 |
| 82 | 0.97 | 0.96 | 0.95 | 0.94 | 0.93 |
| 81 | 0.96 | 0.93 | 0.91 | 0.90 | 0.90 |
| 80 | 0.93 | 0.90 | 0.88 | 0.87 | 0.86 |
| 79 | 0.91 | 0.87 | 0.85 | 0.84 | 0.83 |
| 78 | 0.89 | 0.84 | 0.82 | 0.80 | 0.80 |
| 77 | 0.87 | 0.81 | 0.78 | 0.77 | 0.76 |
| 76 | 0.84 | 0.78 | 0.75 | 0.74 | 0.73 |
| 75 | 0.82 | 0.75 | 0.72 | 0.71 | 0.70 |
| 74 | 0.79 | 0.72 | 0.69 | 0.68 | 0.67 |
| 73 | 0.76 | 0.69 | 0.66 | 0.65 | 0.64 |
| 72 | 0.74 | 0.66 | 0.63 | 0.62 | 0.61 |
| 71 | 0.71 | 0.63 | 0.60 | 0.59 | 0.58 |
| 70 | 0.68 | 0.60 | 0.57 | 0.56 | 0.55 |
| 69 | 0.65 | 0.57 | 0.54 | 0.53 | 0.52 |
| 68 | 0.62 | 0.54 | 0.51 | 0.50 | 0.49 |
| 67 | 0.59 | 0.51 | 0.47 | 0.47 | 0.46 |
| 66 | 0.56 | 0.48 | 0.45 | 0.44 | 0.44 |


|  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $P_{\cup}$ or $P_{L}$ percent <br> Within Limits for <br> Positive Values of <br> $Q_{U}$ or $Q_{L}$ |  |  |  |  |  |
|  | $n=3$ | $n=4$ | $n=5$ | $n=6$ | $n=7$ |
| 65 | 0.52 | 0.45 | 0.43 | 0.41 | 0.41 |
| 64 | 0.49 | 0.42 | 0.40 | 0.39 | 0.38 |
| 63 | 0.46 | 0.39 | 0.37 | 0.36 | 0.35 |
| 62 | 0.43 | 0.36 | 0.34 | 0.33 | 0.32 |
| 61 | 0.39 | 0.33 | 0.31 | 0.30 | 0.30 |
| 60 | 0.36 | 0.30 | 0.28 | 0.27 | 0.27 |
| 59 | 0.32 | 0.27 | 0.25 | 0.25 | 0.24 |
| 58 | 0.29 | 0.24 | 0.23 | 0.22 | 0.21 |
| 57 | 0.25 | 0.21 | 0.20 | 0.19 | 0.19 |
| 56 | 0.22 | 0.18 | 0.17 | 0.16 | 0.16 |
| 55 | 0.18 | 0.15 | 0.14 | 0.13 | 0.13 |
| 54 | 0.14 | 0.12 | 0.11 | 0.11 | 0.11 |
| 53 | 0.11 | 0.09 | 0.08 | 0.08 | 0.08 |
| 52 | 0.07 | 0.06 | 0.06 | 0.05 | 0.05 |
| 51 | 0.04 | 0.03 | 0.03 | 0.03 | 0.03 |
| 50 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |

>Upper Percent Area = 100\%
>Lower Percent Area = 89\%
$>$ The Total Area, the Quality Level, is equal to:

$>$ Note that was the same area as we found with the 1000 samples!

## Pay Factor Calculations

>Finally, we use the Quality Level to determine Pay Factors for the contractor.
$>$ Table 113.1-2 in the Standard Specifications Book shows a Pay Factor of 1.03 for a QL = 89\%.

## Table 113.1-2 Pay Factors

| Pay <br> Factor | Required Quality Level for a Given Sample Size n and Pay Factor |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{n}=3$ | $\mathrm{n}=4$ | $\mathrm{n}=5$ | $\mathrm{n}=\mathbf{6}$ | $\mathrm{n}=7$ |  |
| 1.05 | 100 | 100 | 100 | 100 | 100 |  |
| 1.04 | 90 | 91 | 92 | 93 | 93 |  |
| 1.03 | 80 | 85 | 87 | 88 | 89 |  |
| 1.02 | 75 | 80 | 83 | 85 | 86 |  |
| 1.01 | 71 | 77 | 80 | 82 | 84 |  |
| 1.00 | 68 | 74 | 78 | 80 | 81 |  |
| 0.99 | 66 | 72 | 75 | 77 | 79 |  |
| 0.98 | 64 | 70 | 73 | 75 | 77 |  |
| 0.97 | 62 | 68 | 71 | 74 | 75 |  |
| 0.96 | 60 | 66 | 69 | 72 | 73 |  |
| 0.95 | 59 | 64 | 68 | 70 | 72 |  |
| 0.94 | 57 | 63 | 66 | 68 | 70 |  |
| 0.93 | 56 | 61 | 65 | 67 | 69 |  |
| 0.92 | 55 | 60 | 63 | 65 | 67 |  |
| 0.91 | 53 | 58 | 62 | 64 | 66 |  |
| 0.90 | 52 | 57 | 60 | 63 | 64 |  |
| 0.89 | 51 | 55 | 59 | 61 | 63 |  |
| 0.88 | 50 | 54 | 57 | 60 | 62 |  |
| 0.87 | 48 | 53 | 56 | 58 | 60 |  |
| 0.86 | 47 | 51 | 55 | 57 | 59 |  |
| 0.85 | 46 | 50 | 53 | 56 | 58 |  |
| 0.84 | 45 | 49 | 52 | 55 | 56 |  |
| 0.83 | 44 | 48 | 51 | 53 | 55 |  |
| 0.82 | 42 | 46 | 50 | 52 | 54 |  |
| 0.81 | 41 | 45 | 48 | 51 | 53 |  |
| 0.80 | 40 | 44 | 47 | 50 | 52 |  |
| 0.79 | 38 | 43 | 46 | 48 | 50 |  |
| 0.78 | 37 | 41 | 45 | 47 | 49 |  |
| 0.77 | 36 | 40 | 43 | 46 | 48 |  |
| 0.76 | 34 | 39 | 42 | 45 | 47 |  |
| 0.75 | 33 | 38 | 41 | 44 | 46 |  |

## Maximum Pay Factor

> Base and Subbase - 1.00
$>$ Treated Base - 1.00
> Plant Mix Pavement - 1.05
> Plant Mix Wearing Course - 1.05
> Seal Coat Aggregate 1.05
$>$ PCCP - 1.00

## Pay Factor Calculation (continued)

## TERMS

$>x-$ an individual test value
$>\Sigma x$ - the summation of test values
$>x-$ the average of a series of test values
$>\mathrm{N}$ - the number of test values
$>$ s - the standard deviation
$>\mathrm{SL}_{\mathrm{u}}$ - the upper specification limit
$>\mathrm{SL}_{\mathrm{L}}$ - the lower specification limit
$>Q_{U}$ - the Upper Quality Index
$>Q_{L}$ - the Lower Quality Index
$>\mathrm{P}_{\mathrm{U}}$ - the percent of material within $\mathrm{SL}_{\mathrm{U}}$
$>\mathrm{P}_{\mathrm{L}}$ - the percent of material within $\mathrm{SL}_{\mathrm{L}}$
$>$ QL - Quality Level - the total percent of material within specifications

## Pay Factor Worksheet - \#1



Table 113.1-1
Quality Level Analysis by the Standard Deviation Method

| $P_{U}$ or $P_{L}$ percent Within Limits for Positive Values of $Q_{U}$ or $Q_{L}$ | Upper Quality Index $Q_{U}$ or Lower Quality Index$Q_{L}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{n}=3$ | $\mathrm{n}=4$ | $\mathrm{n}=5$ | $\mathrm{n}=6$ | $\mathrm{n}=7$ |
| 100 | 1.16 | 1.50 | 1.79 | 2.03 | 2.23 |
| 99 |  | 1.47 | 1.67 | 1.80 | 1.89 |
| 98 | 1.15 | 1.44 | 1.60 | 1.70 | 1.76 |
| 97 |  | 1.41 | 1.54 | 1.62 | 1.67 |
| 96 | 1.14 | 1.38 | 1.49 | 1.55 | 1.59 |
| 95 |  | 1.35 | 1.44 | 1.49 | 1.52 |
| 94 | 1.13 | 1.32 | 1.39 | 1.43 | 1.46 |
| 93 |  | 1.29 | 1.35 | 1.38 | 1.40 |
| 92 | 1.12 | 1.26 | 1.31 | 1.33 | 1.35 |
| 91 | 1.11 | 1.23 | 1.27 | 1.29 | 1.30 |
| 90 | 1.10 | 1.20 | 1.23 | 1.24 | 1.25 |
| 89 | 1.09 | 1.17 | 1.19 | 1.20 | 1.20 |
| 88 | 1.07 | 1.14 | 1.15 | 1.16 | 1.16 |
| 87 | 1.06 | 1.11 | -1.12 | 1.12 | 1.12 |
| 86 | 1.04 | 1.08 | 1.08 | 1.08 | 1.08 |
| 85 | 1.03 | 1.05 | 1.05 | 1.04 | 1.04 |
| 84 | 1.01 | 1.02 | 1.01 | 1.01 | 1.00 |
| 83 | 1.00 | 0.99 | 0.98 | 0.97 | 0.97 |
| 82 | 0.97 | 0.96 | 0.95 | 0.94 | 0.93 |
| 81 | 0.96 | 0.93 | 0.91 | 0.90 | 0.90 |
| 80 | 0.93 | 0.90 | 0.88 | 0.87 | 0.86 |
| 79 | 0.91 | 0.87 | 0.85 | 0.84 | 0.83 |
| 78 | 0.89 | 0.84 | 0.82 | 0.80 | 0.80 |
| 77 | 0.87 | 0.81 | 0.78 | 0.77 | 0.76 |
| 76 | 0.84 | 0.78 | 0.75 | 0.74 | 0.73 |
| 75 | 0.82 | 0.75 | 0.72 | 0.71 | 0.70 |
| 74 | 0.79 | 0.72 | 0.69 | 0.68 | 0.67 |
| 73 | 0.76 | 0.69 | 0.66 | 0.65 | 0.64 |
| 72 | 0.74 | 0.66 | 0.63 | 0.62 | 0.61 |
| 71 | 0.71 | 0.63 | 0.60 | 0.59 | 0.58 |
| 70 | 0.68 | 0.60 | 0.57 | 0.56 | 0.55 |
| 69 | 0.65 | 0.57 | 0.54 | 0.53 | 0.52 |
| 68 | 0.62 | 0.54 | 0.51 | 0.50 | 0.49 |
| 67 | 0.59 | 0.51 | 0.47 | 0.47 | 0.46 |
| 66 | 0.56 | 0.48 | 0.45 | 0.44 | 0.44 |


|  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $P_{\cup}$ or $P_{L}$ percent <br> Within Limits for <br> Positive Values of <br> $Q_{U}$ or $Q_{L}$ |  |  |  |  |  |
|  | $n=3$ | $n=4$ | $n=5$ | $n=6$ | $n=7$ |
| 65 | 0.52 | 0.45 | 0.43 | 0.41 | 0.41 |
| 64 | 0.49 | 0.42 | 0.40 | 0.39 | 0.38 |
| 63 | 0.46 | 0.39 | 0.37 | 0.36 | 0.35 |
| 62 | 0.43 | 0.36 | 0.34 | 0.33 | 0.32 |
| 61 | 0.39 | 0.33 | 0.31 | 0.30 | 0.30 |
| 60 | 0.36 | 0.30 | 0.28 | 0.27 | 0.27 |
| 59 | 0.32 | 0.27 | 0.25 | 0.25 | 0.24 |
| 58 | 0.29 | 0.24 | 0.23 | 0.22 | 0.21 |
| 57 | 0.25 | 0.21 | 0.20 | 0.19 | 0.19 |
| 56 | 0.22 | 0.18 | 0.17 | 0.16 | 0.16 |
| 55 | 0.18 | 0.15 | 0.14 | 0.13 | 0.13 |
| 54 | 0.14 | 0.12 | 0.11 | 0.11 | 0.11 |
| 53 | 0.11 | 0.09 | 0.08 | 0.08 | 0.08 |
| 52 | 0.07 | 0.06 | 0.06 | 0.05 | 0.05 |
| 51 | 0.04 | 0.03 | 0.03 | 0.03 | 0.03 |
| 50 | 0.00 | 0.00 | 0.00 | 0.00 | 0.00 |

## Table 113.1-2 Pay Factors

| Pay <br> Factor | Required Quality Level for a Given Sample Size n and Pay Factor |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{n}=3$ | $\mathrm{n}=4$ | $\mathrm{n}=5$ | $\mathrm{n}=6$ | $\mathrm{n}=7$ |  |
| 1.05 | 100 | 100 | 100 | 100 | 100 |  |
| 1.04 | 90 | 91 | 92 | 93 | 93 |  |
| 1.03 | 80 | 85 | 87 | 88 | 89 |  |
| 1.02 | 75 | 80 | 83 | 85 | 86 |  |
| 1.01 | 71 | 77 | 80 | 82 | 84 |  |
| 1.00 | 68 | 74 | 78 | 80 | 81 |  |
| 0.99 | 66 | 72 | 75 | 77 | 79 |  |
| 0.98 | 64 | 70 | 73 | 75 | 77 |  |
| 0.97 | 62 | 68 | 71 | 74 | 75 |  |
| 0.96 | 60 | 66 | 69 | 72 | 73 |  |
| 0.95 | 59 | 64 | 68 | 70 | 72 |  |
| 0.94 | 57 | 63 | 66 | 68 | 70 |  |
| 0.93 | 56 | 61 | 65 | 67 | 69 |  |
| 0.92 | 55 | 60 | 63 | 65 | 67 |  |
| 0.91 | 53 | 58 | 62 | 64 | 66 |  |
| 0.90 | 52 | 57 | 60 | 63 | 64 |  |
| 0.89 | 51 | 55 | 59 | 61 | 63 |  |
| 0.88 | 50 | 54 | 57 | 60 | 62 |  |
| 0.87 | 48 | 53 | 56 | 58 | 60 |  |
| 0.86 | 47 | 51 | 55 | 57 | 59 |  |
| 0.85 | 46 | 50 | 53 | 56 | 58 |  |
| 0.84 | 45 | 49 | 52 | 55 | 56 |  |
| 0.83 | 44 | 48 | 51 | 53 | 55 |  |
| 0.82 | 42 | 46 | 50 | 52 | 54 |  |
| 0.81 | 41 | 45 | 48 | 51 | 53 |  |
| 0.80 | 40 | 44 | 47 | 50 | 52 |  |
| 0.79 | 38 | 43 | 46 | 48 | 50 |  |
| 0.78 | 37 | 41 | 45 | 47 | 49 |  |
| 0.77 | 36 | 40 | 43 | 46 | 48 |  |
| 0.76 | 34 | 39 | 42 | 45 | 47 |  |
| 0.75 | 33 | 38 | 41 | 44 | 46 |  |
|  |  |  |  |  |  |  |

## Maximum Pay Factor <br> $>$ Base and Subbase - 1.00

> Treated Base - 1.00
$>$ Plant Mix Pavement - 1.05
$>$ Plant Mix Wearing Course - 1.05
$>$ Seal Coat Aggregate 1.05
$>$ PCCP - 1.00

## Pay Factor Worksheet - \#2

Aggregate Specification:
Crushed Base Grading W
$n=$ $\qquad$ $45 \quad 53$

57
62
Test Values:
Average Value:
$\bar{x}=$ $\qquad$

$$
\begin{gathered}
s= \\
\left(\sigma_{\mathrm{n}-1}\right)
\end{gathered}
$$

$\qquad$

Upper Specification Limit, SL $_{U}=$ $\qquad$ Lower Specification Limit, $\mathrm{SL}_{\mathrm{L}}=$ $\qquad$
Upper Quality Index

$$
\mathbf{Q}_{U}=\frac{S L_{U}-\overline{\mathbf{x}}}{s}
$$

$$
\mathbf{P}_{\mathrm{U}}=
$$

$\qquad$ (From Table 113.1-1) (If $S L_{U}$ is not specified, $P_{U}=100$ )

Lower Quality Index,

$$
\mathbf{Q}_{\mathrm{L}}=\frac{\overline{\mathbf{x}}-\mathrm{SL}_{\mathrm{L}}}{\mathbf{s}}
$$

Percent Material Within $\mathrm{SL}_{\mathrm{L}}$
$\mathrm{P}_{\mathrm{L}}=$ $\qquad$ (From Table 113.1-1)
(If $\mathrm{SL}_{\mathrm{L}}$ is not specified, $\mathrm{P}_{\mathrm{L}}=100$ )

Quality Level = Percent Within Specification Limits


## Pay Factor Worksheet - \#3

## Test Results:

Test Values:
Average Value:

| $\mathrm{n}=$ | 5 |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 3.1 | 4.9 | 6.7 | 7.1 | 5.9 |

$\overline{\mathrm{x}}=$ $\qquad$
$\qquad$
Upper Specification Limit, $\mathrm{SL}_{\mathrm{U}}=$ $\qquad$
Lower Specification Limit, $\mathrm{SL}_{\mathrm{L}}=$ $\qquad$

Percent Material Within $S L_{L}$
(If $S L_{L}$ is not specified, $P_{L}=100$ )
Quality Level $=$ Percent Within Specification Limits
$\mathrm{QL}=\left(\mathrm{P}_{\mathrm{U}}+\mathrm{P}_{\mathrm{L}}\right)-100=$ $\qquad$ $+$ $\qquad$ $-100=$ $\qquad$
Pay Factor $=$ PF =

(From Table 113.1-2)
Max Pay Factor=
Minimum Pay Factor $=$ $\qquad$
Pay Adjustment Factor = PAF
$=$ Min Pay Factor - $1.00=$
$-1.00=$ $\qquad$

## Pay Factor

## Additional Stipulations

$>$ Lots consist of 3 to 7 samples but usually 5
$>$ Contractor samples - Engineer directs
$>$ Sample size $\geq 30$ lbs
$>P F$ for lot $=$ lowest $P F$ for any sieve
$>$ Does not apply to 97 - 100 or 95 - 100
> Minimum acceptable PF - 0.75

## Pay Factor (continued)

$>$ Reject material removed
$>$ Obviously defective material - rejected and removed
>2 Consecutive Lots < 1.00 PF - Adjustments
$>$ Contractor may remove and replace to avoid penalty

## Pay Factor Calculations

$>100$ Tons of Plant Mix Aggregate
> $\$ 15.00$ per Ton
$>$ Minimum Payment Adjustment Factor PAF = +0.02
$>$ Regular Payment =
(100 Tons)(\$15.00/Ton) = \$1500
$>$ Bonus for Quality Aggregate $=$ (+0.02)(\$1500) = \$30.00
$>$ Total Payment $=\mathbf{\$ 1 5 3 0 . 0 0}$

## Maximum Pay Factors

$>$ Base and Subbase - 1.00
$>$ Treated Base - 1.00
>Plant Mix Pavement - 1.05
$>$ Plant Mix Wearing Course-1.05
$>$ Seal Coat Aggregate - 1.05
$>$ PCCP - 1.00

